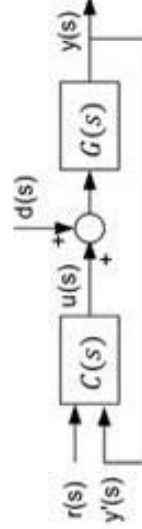


## ABSTRACT

- A multi-stage approach is proposed merging a deterministic and evolutionary algorithm [1] for PI controller tuning.
- This technique is formulated through the design of a multi-objective optimization procedure, to ensure the construction of a Pareto frontier that guarantees a well distribution and exclude the non-Pareto and local Pareto points.
- This procedure focuses on reliability-based optimization instances.

## PI CONTROL SYSTEM

The process under consideration is the *Control Benchmark 2012* described by [2]. The control of boilers has been an important problem for a long time. The process will be controlled by a proportional-integral controller (PI). A conventional control scheme is assumed:



The identified nominal model to be used is:

$$G(s) = \frac{0.3934}{1+45.6794s} e^{-3.42s}$$

This model was obtained with a step response experiment using the standard identification toolbox from Matlab® with a standard step response.

## SYSTEM REQUIREMENTS

The objectives design for the controller tuning, according to the control loop are:

- $J_1(\theta)$ : the most natural way to measure the performance is the integrated-absolute-error (IAE).
- $J_2(\theta)$ : some results in [3] show that we can directly associate the robustness ( $M_r$ ) to the performance index (TV) in such a way, we will have a single index which gives a measure for the input usage and system robustness.
- $J_3(\theta)$ : Reliability based optimization instances concern is to guarantee a given performance by minimizing the nominal performance degradation when we consider a set of potential models instead of a singleton such a style nominal model.

## ACKNOWLEDGMENT

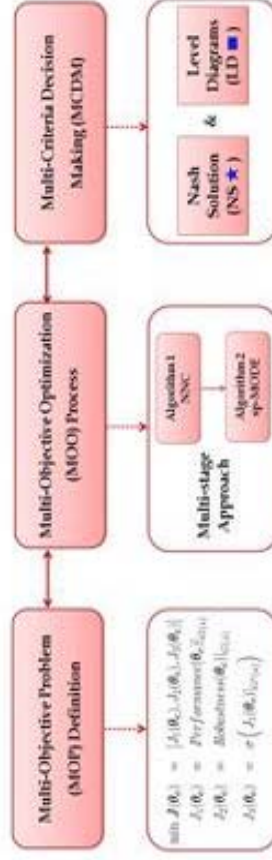
This work was partially supported by the Spanish Ministry of Economy and Competitiveness program under grant DPI2013-47825-C3-1-R and by the National Council of Scientific and Technological Development of Brazil (CNPq) with the fellowship BJT-304804/2014-2.

## REFERENCES

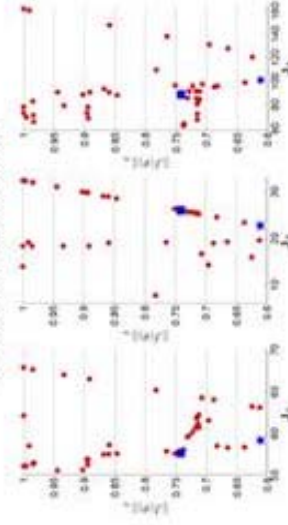
- [1] G. Reynoso-Meza, "NNC algorithm for multi-objective optimization & Multiobjective Differential Evolution Algorithm with Spherical Pruning." Both algorithms are available in Matlab Central.
- [2] Fernando Morilla, "Benchmark for PID control based on the boiler control problem." Internal report, UNED Spain-2012.
- [3] H.S. Sánchez, R. Vilanova, "Multiobjective tuning of PI controller using the NNC Method: Simplified problem definition and guidelines for decision making." 18th IEEE Conference on Emerging Technologies & Factory Automation (ETFA), 10-13 September, Cagliari, Italy, 2013.

## METHODOLOGY

### Multi-objective Optimization Design (MOOD) Procedure



Pareto Front approximation

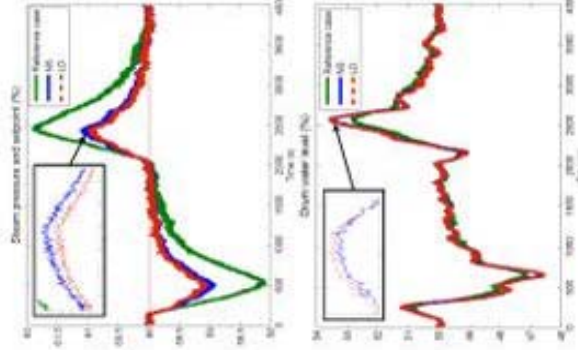


Two solutions were selected from the Pareto front:

- NS  $\{\theta_c\} = [2.31, 22.16]$
- LD  $\{\theta_c\} = [2.54, 21.25]$

## RESULTS & DISCUSSIONS

- Test type 1: Performance of the PI controller selected with the NS ( $J_b = 0.8616$ ), LD ( $J_b = 0.8464$ ) and its comparison with the reference case in the benchmark setup.



- Test type 2: Performance of the PI controller selected with the NS ( $J_b = 0.8325$ ), LD ( $J_b = 0.8161$ ) and its comparison with the reference case in the benchmark setup.

## CONCLUSION

The approach has been shown effective by its application to a Boiler Benchmark problem; bringing a good approximation of the Pareto front, ensure the accurate convergence and diversity. As it can be noticed both design alternative bring an effective controller that fulfill all the requirements, with a better performance than the reference controller. It seems that the multistage approach brings a suitable framework and also includes the reliability on MOOD procedure.